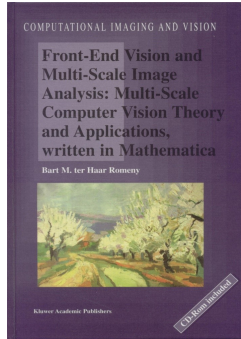


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**From the book:**

**ter Haar Romeny, B. M.:**

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written in Mathematica.**

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